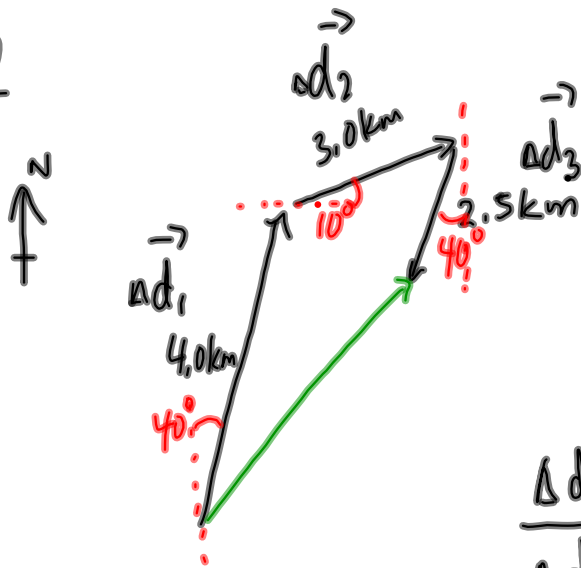


PP/110

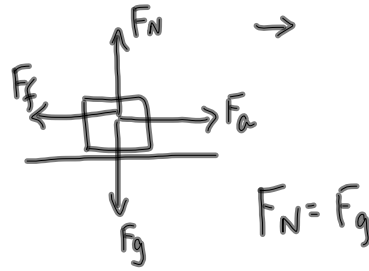
26.



	x	y
Δd_1		
Δd_2		
Δd_3		
$\Delta \vec{d}$		

Forces at Angles

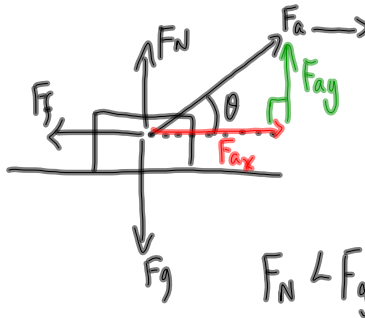
Horizontal Force
Horizontal Surface



F_N is always perpendicular to the surface.

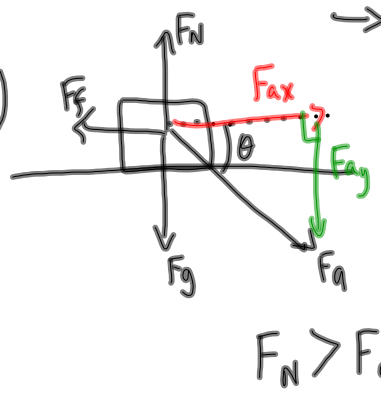
Horizontal Surface

Force is upward at an angle (pulling) a toboggan



Horizontal Surface

Force is downward at an angle (pushing a lawn mower)

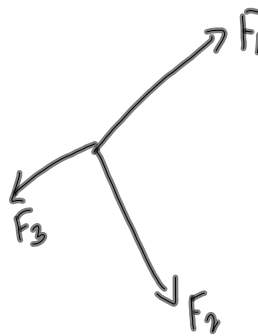


Three way Tug of War

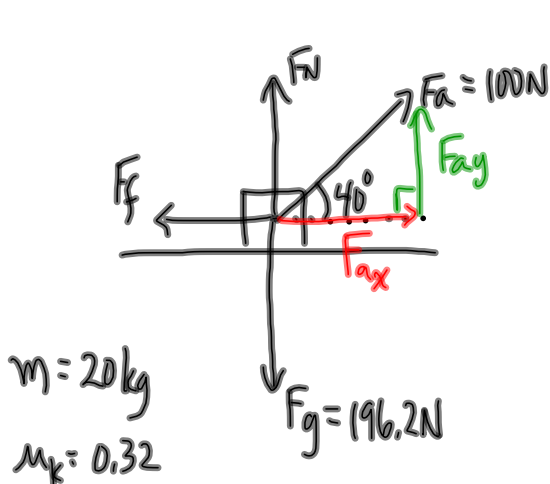
Bird's Eye View:



$F_g = F_N$ as long as all 3 forces are parallel to the plane.



SP



$m = 20\text{ kg}$
 $\mu_k = 0.32$

$\rightarrow (\vec{F}_N + \vec{F}_{ay} + \vec{F}_g = 0)$

Vertically $(\vec{F}_{net} = 0)$

$F_N + F_{ay} = F_g$

$F_N = F_g - F_{ay}$

$F_N = 196.2\text{ N} - 64.28\text{ N}$

$F_N = 131.92\text{ N}$

$\cos \theta = \frac{\text{adj}}{\text{hyp}}$

$\sin \theta = \frac{\text{opp}}{\text{hyp}}$

$\cos 40^\circ = \frac{F_{ax}}{100\text{ N}}$

$\sin 40^\circ = \frac{F_{ay}}{100\text{ N}}$

$F_{ax} = 100\text{ N} \cos 40^\circ$

$F_{ay} = 100\text{ N} \sin 40^\circ$

76.60 N

64.28 N

Horizontally:

$\vec{F}_{net} = m\vec{a}$

$F_{ax} - F_f = ma$

$F_{ax} - \mu F_N = ma$

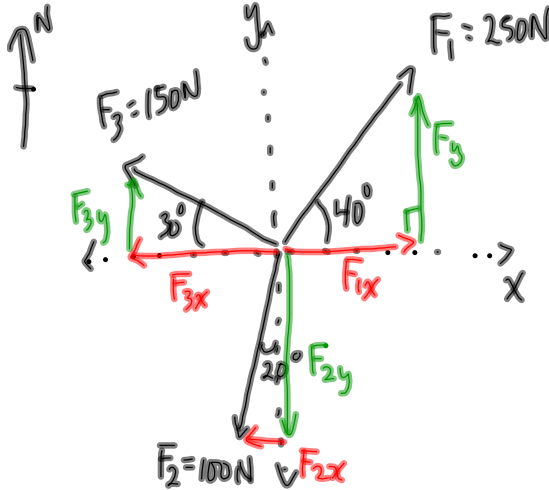
$76.60\text{ N} - 0.32(131.92\text{ N}) = (20\text{ kg})a$

$34.39\text{ N} = (20\text{ kg})a$

$a = 1.7\text{ m/s}^2$

Three-Way Tug of War

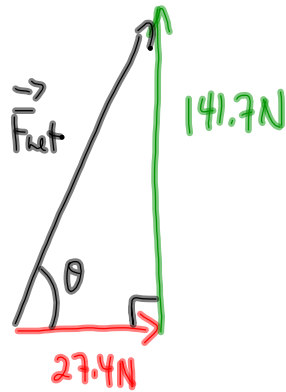
Bird's Eye View



This is a FBD

NOT
A vector addition diagram (head-tail)

	x	y
F_1	$(250N) \cos 40^\circ$ 191.5	$(250N) \sin 40^\circ$ 160.7
F_2	$-(100N) \sin 20^\circ$ -34.2	$-(100N) \cos 20^\circ$ -94.0
F_3	$-(150N) \cos 30^\circ$ -129.9	$(150N) \sin 30^\circ$ 75
F_{net}	27.4 N	141.7 N



$$c^2 = a^2 + b^2$$

$$c^2 = (27.4)^2 + (141.7)^2$$

$$c = 144 \text{ N}$$

$$\tan \theta = \frac{141.7N}{27.4N}$$

$$\theta = 79^\circ$$

$$\vec{F}_{net} = 144N [\text{E } 79^\circ \text{ N}]$$